

An empirical analysis of machine learning models for automated essay grading

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Background. Automated Essay Scoring (AES) is an area which falls at the intersection of computing and linguistics. AES systems conduct a linguistic analysis of a given essay or prose and then estimates the writing skill or the essay quality in the form a numeric score or a letter grade. AES systems are useful for the school, university and testing company community for efficiently and effectively scaling the task of grading a large number of essays.

Methods. We propose an approach for automatically grading a given essay based on 9 surface level and deep linguistic features, 2 feature selection and ranking techniques and 4 text classification algorithms. We conduct a series of experiments on publicly available manually graded and annotated essay data and demonstrate the effectiveness of our approach. We investigate the performance of two different features selection techniques (1) RELIEF (2) Correlation-based Feature Subset Selection (CFS) with three different machine learning classifiers (kNN, SVM and Linear Regression). We also apply feature normalization and scaling.

Results. Our results indicate that features like world count with respect to the world limit, appropriate use of vocabulary, relevance of the terms in the essay with the given topic and coherency between sentences and paragraphs are good predictors of essay score. Our analysis reveals that not all features are equally important and few features are more relevant and better correlated with respect to the target class. We conduct experiments with k-nearest neighbour, logistic regression and support vector machine based classifiers. Our results on 4075 essays across multiple topics and grade score range are encouraging with an accuracy of 73% to 93%.

Discussion. Our experiments and approach are based on Grade 7 to Grade 10 essays which can be generalized to essays from other grades and level after doing context specific customization. Few features are more relevant and important than other features and it is interplay or combination of multiple feature values which determines the final score. We observe that different classifiers result in difference accuracy.

1 An Empirical Analysis of Machine Learning 2 Models for Automated Essay Grading

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9 ABSTRACT

10 **Background.** Automated Essay Scoring (AES) is an area which falls at the intersection of computing
11 and linguistics. AES systems conduct a linguistic analysis of a given essay or prose and then estimates
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16 deep linguistic features, 2 feature selection and ranking techniques and 4 text classification algorithms.
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25 important and few features are more relevant and better correlated with respect to the target class. We
26 conduct experiments with k-nearest neighbour, logistic regression and support vector machine based
27 classifiers. Our results on 4075 essays across multiple topics and grade score range are encouraging
28 with an accuracy of 73% to 93%.

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30 generalized to essays from other grades and level after doing context specific customization. Few features
31 are more relevant and important than other features and it is interplay or combination of multiple feature
32 values which determines the final score. We observe that different classifiers result in difference accuracy.

33 1 INTRODUCTION

34 1.1 Research Motivation and Aim

35 Automated Essay Grading or Scoring (AEG or AES) consists of automatically evaluating the score or
36 grade of a written essay (Cummins et al., 2016)(Dong and Zhang, 2016) (Balfour, 2013) (Chen et al.,
37 2010). AES systems are motivated by the need to develop solutions for assisting teachers in grading
38 essays in an efficient and effective manner. AES systems are also useful for students to understand issues
39 in their writing by receiving a quick feedback from a system rather than waiting for inputs from a teacher.
40 Accurate and reliable AES systems are needed by schools, universities and testing companies to be able
41 to manage the grading of essays by large number of students. One of the main technical challenges in
42 building an AES system is to be able to achieve an output which is in agreement with a human evaluator.
43 AES systems has attracted the attention of several researchers and several solution approaches have been
44 proposed (Cummins et al., 2016)(Dong and Zhang, 2016) (Balfour, 2013) (Chen et al., 2010). However,
45 AES is still not a fully solved problem and we believe more research and alternative novel approaches are
46 needed to further enhance the state-of-the-art. Our research work presented in this paper is motivated
47 by the need to conduct experiment on the effectiveness of several linguistic features and variables for

48 estimating the score of an essay written primarily by middle school students. While the framework and
49 methodology presented in our work can be generalized, our focus is on grading essays of school students
50 from Grade 7 to Grade 10. Our motivation is to investigate whether writing skills can be assessed by
51 automatically checking aspects such as richness in vocabulary, word count with respect to the prescribed
52 limit, semantic similarity of the terms in essay with the topic of the prose, usage of active and passive
53 voice, semantic similarity and coherence of terms in the essay body, spelling errors, usage of tense,
54 grammatical errors and sentence lengths.

55 There are several research gaps and open research questions in the area of automated essay scoring and
56 grading. One the research questions pertains to identification of relevant and important textual features
57 which can be used to predict the writing skill of the student and quality of the essay. Our aim is to
58 investigate 9 different features for automated essay scoring task. Few of the features are surface level
59 and few require a deeper natural language processing. Our aim is to investigate the effectiveness of 9
60 features in which few are positively correlated to quality and few are negatively correlated. Conducting
61 experiments on 9 surface level and deep features, positively and negatively correlated features with the
62 score is one of the unique contributions of our work. Our aim is to understand whether our proposed 9
63 features can be considered as proxies to determine the quality of a student essay at the middle school level.
64 Information retrieval, natural language processing and machine learning have applied several techniques
65 and computational tools (refer to the Literature Survey and Related Work Section of this paper) for
66 computing the score of a given essay. Machine learning is a vast area consisting of several algorithms and
67 methods. Our research aim is to examine the performance of algorithms (and combination of algorithms
68 in a data processing pipeline) which are relatively unexplored. Our aim is to investigate the performance
69 of two different features selection techniques (1) RELIEF (2) Correlation-based Feature Subset Selection
70 (CFS) with three different machine learning classifiers (kNN, SVM and Linear Regression). The main
71 research contributions of our work in context to the existing work on AES is the application of 9 surface
72 level and deep linguistic features, 2 feature selection techniques, 3 classification algorithms on 3 real-
73 world manually annotated publicly available dataset for the task of automatically grading essays. We
74 conduct a series of experiments and conduct a focused and in-depth analysis of our proposed solution
75 approach.

76 1.2 Literature Survey and Related work

77 Automated essay scoring and assessment is an important and a technically challenging task and hence
78 attracted the attention of several researchers in the area of machine learning and information retrieval. In
79 this Section, we present several closely related work to our research presented in this paper. Cummins
80 et al. present a constrained multi-task learning approach for automated essay scoring (Cummins et al.,
81 2016). They develop a ranking model using several features such as essay length, grammatical relations,
82 max-word length and min-sentence length and part-of-speech counts (Cummins et al., 2016). Dong et
83 al. propose an approach based on neural networks for automatically learning features for the task of
84 automated essay scoring (Dong and Zhang, 2016). They compare the effectiveness of automatically
85 induced features with handcrafted features and conclude that automatically induced features results
86 in good performance (Dong and Zhang, 2016). Yannakoudakis et al. use rank preference learning
87 to explicitly model the grade relation between answer scripts (Yannakoudakis et al., 2011). The rank
88 reference system achieves performance close to the upper bound of the task of grading ESOL texts
89 (Yannakoudakis et al., 2011).

90 Ross et al. use machine learning SIDE program to automatically evaluate the accuracy of 565 students'
91 written explanation of evolutionary change (Nehm et al., 2012). Using Kappa inter-rater agreement
92 between the program and human rater, the SIDE performance was found most effective when scoring
93 models were built using individual item level (Nehm et al., 2012). In subject specific essays such as Life
94 Sciences, Ross et al. investigate the impact of misspelled words on scoring accuracy of a model (Ha and
95 Nehm, 2016). They establish that misspelled words have a greater impact on naive ideas as compared to
96 key concepts and false positive feedback (Ha and Nehm, 2016). Balfour et al. compares human based
97 UCLA's calibrated peer review (CPR) with the Automated Scoring System(AES) (Balfour, 2013). They
98 reason that for several types of essays, AES gives immediate feedback while CPR is better applied to
99 train students with Evaluation Skills (Balfour, 2013). Rudner et. al provide two-part evaluation of the
100 Intellimetric scoring system for Analytical Writing Assessment in GMAT (Rudner et al., 2006). Using a
101 weighted probability model, they infer Pearson r-correlations of agreement between human raters and the

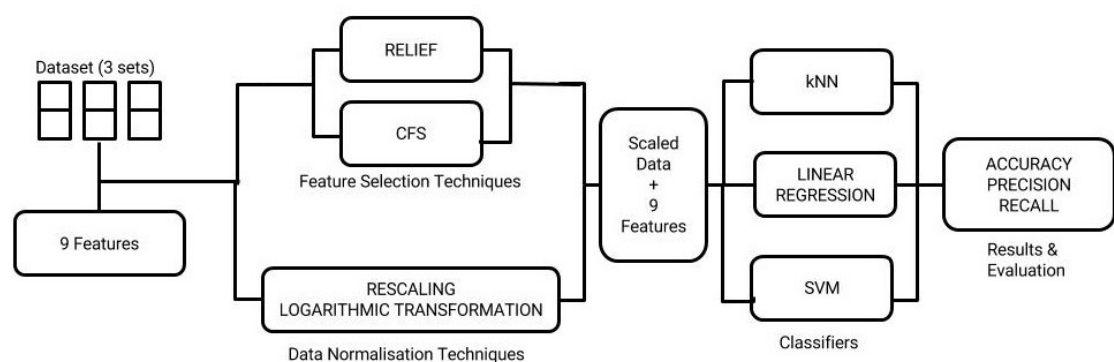
102 IntelliMetric system averaged .83 in both evaluations (Rudner et al., 2006).

103 Bin et al made use of the kNN algorithm to categorise essays (Bin et al., 2008). They first converted
 104 essays into vectors in a VSM and after filtering out the stop words, employed the Information Gain
 105 technique to conduct feature selection. They observed that the best results are given by $k = 3$ and $k = 5$
 106 and that words and phrases give poorer results as compared to arguments (Bin et al., 2008). Kakkonen
 107 et al employed Probabilistic Latent Semantic Analysis (PLSA) and Latent Semantic Analysis (LSA)
 108 techniques to grade essays written in Finnish by setting the similarity metric as the cosine of the angle
 109 (Kakkonen et al., 2005). They concluded that although LSA's and PLSA's performances were similar, the
 110 former performed marginally better than the latter (Kakkonen et al., 2005). McNamara et al. made use of
 111 three techniques for grading essays: Coh-Matrix, the Writing Analysis Tool and the Linguistic Inquiry
 112 and Word Count (McNamara et al., 2015). They carried out correlations between the variables reported by
 113 the three techniques and then employed various filtering methods to reduce the number of variables from
 114 320 to 140. Next, a discriminant function analysis (DFA) model was used whose accuracy was judged
 115 based on: chi-square, Pearson r , Cohen's Kappa, exact accuracy, and adjacent accuracy (McNamara et al.,
 116 2015). Chen et al. propose an unsupervised approach to essay grading by focusing on the similarity
 117 between essays rather than assuming any prior score information (Chen et al., 2010). They employed the
 118 voting algorithm and concluded by observing the limited scope of the bag of words model, especially in
 119 the domain of creative writing (Chen et al., 2010).

120 2 MATERIALS AND METHOD

121 2.1 Research Framework and Solution Approach

122 Figure 1 shows the research framework and solution approach for our automatic essay grading system. As
 123 shown in the Figure 1, the framework consists of 3 sets of data (separate training and test dataset for each
 124 of the 3 sets), data scaling and normalization technique, two feature selection techniques (RELIEF and
 125 CFS), three classification techniques (kNN, linear regression, SVM) and performance evaluation metrics.
 126 We use the publicly available dataset from Kaggle¹ so that our experiments can be easily replicated and
 127 can be used for comparison with other approaches. The dataset consists of several essays having an
 128 average length 150 to 550 words. The essays are written by middle school students from Grade 7 to Grade
 129 10. We propose and implement 9 features. The 9 features are: Vocabulary, Word Count Limit Ratio,
 130 Semantic Similarity Topic Essay, Voice, Semantic Similarity Essay, Spell Errors, Tense, Grammatical
 131 Errors and Long Sentences. We apply feature scaling and normalization before providing it as input to the
 132 machine learning algorithm. We need to rescale the values as the scale and range for all the features are
 different. Following is the brief description of the proposed 9 features.



133 **Figure 1.** High Level Solution Approach and Research Framework Diagram

134 **Word Count Ratio** This feature calculates the ratio of the word count of the given essay with respect to
 135 the specified word limit. Our objective is to measure how far the given essay is from the specified
 136 word limit in terms of the extent to which the given essay being either too many or too few words.

¹<https://www.kaggle.com/c/asap-aes>

137 This feature assumes equal weightage for equal number of words above or below the word limit.
138 This feature uses Python library textstat² to tokenise and count the number of words in the document.
139 The score for this feature is calculated as : $(1-WC/WL)$ where WC represents the word count of
140 the given essay and WL represents the world limit provided in the essay guideline. Subtracting the
141 ratio from 1 is a way of normalising the score (equivalent to taking absolute value of the ratio).

142 **Sentence Length** Research shows that very long sentences are hard to comprehend and hence less
143 effective and less coherent due to their high verbosity. Presence of many long sentences negatively
144 impact the final grade of the essay. This feature computes the number of long sentences. We use
145 our word count feature discussed above. We use the Python NLTK library³ to tokenise the text
146 into sentences and count the total number of sentences. The score for this feature is calculated by
147 dividing the number of sentences having 15 or more words by the total number of sentences in the
148 essay. A large ratio implies that an average sentence of the essay is long.

149 **Voice of the Essay** Essay graders recommend that any piece of writing or prose be in active voice rather
150 than passive voice for a better coherency and comprehension. This feature evaluates to what extent
151 sentences in the given essay has been consistently written in active or passive voice. For computing
152 the value of this feature, we use SpaCy Python toolkit⁴ to identify the voice of a sentence by
153 analysing the structure of the sentence. For example, in active voice, the subject performs the active
154 verb's action whereas in passive voice, the subject gets acted upon by the verb's action (which is no
155 longer active). The score for this feature is calculated by dividing the number of sentences written
156 in active voice by the total number of sentences in the given essay. A large ratio suggests that an
157 average sentence in the essay is written in active voice.

158 **Tense of the Essay** Essay graders and educators recommend that a good piece of writing should be
159 written consistently in the same tense (regardless of the choice of tense). Mixing different tenses
160 may result in a negative impact on the final grade as it makes the essay difficult to comprehend and
161 understand. This feature uses the NLTK Python library to identify different parts of speech (such
162 as verbs, nouns, adjectives) and focusses mainly on verbs. The score for this feature is calculated
163 by first determining what is the dominant tense verb in the essay? Further calculation is done by
164 dividing the number of such verbs by the total number of verbs. A large ratio implies that there is
165 one dominant tense in the essay which is positively correlated with good writing skills and score.

166 **Spell Check** It is natural that a good piece of writing minimises the number of spelling errors. This
167 feature first tokenises the text into words and then uses Enchant spell checking library⁵ to look up
168 the spelling of these words and returns a count of the number of spelling errors occurring in the
169 document. The score for this feature is calculated by dividing the number of spelling errors by the
170 total number of words in the document. A large ratio suggests a high number of spelling mistakes,
171 which has a negative influence and correlation with the essay score.

172 **Grammatical Errors** Similar to spelling errors, it is natural that grammatical errors reduces the essay
173 quality and comprehension. We compute the proportion of grammatical errors in the document
174 by using language-check module in Python⁶. For each sentence, language check checks whether
175 the sentence follows certain grammatical rules or not. The score for this feature is calculated by
176 dividing the number of grammatical errors by the total number of words in the document. A large
177 ratio implies a large number of grammatical errors. A large ration is negatively correlated with the
178 essay score.

179 **Vocabulary** Using a rich vocabulary and appropriate vocabulary usage is a good indicator of writing
180 quality. Good organization of ideas and creating a syntactic variety requires good vocabulary. This
181 feature employs a bag of words model. We use the NLTK Python library to first tokenise the text
182 into words and then remove all the stop words and returns the count of unique words. The score for
183 this feature is calculated by dividing the number of unique words by the word limit. The rationale

²<https://pypi.python.org/pypi/textstat/0.1.4>

³<http://www.nltk.org/>

⁴<https://spacy.io/>

⁵<https://www.abisource.com/projects/enchant/>

⁶https://bitbucket.org/spirit/language_tool

184 behind using word limit (rather than word count) is to take care of cases where the ratio may be
185 high owing to the fact that the essay had very few words (essays which are much shorter than the
186 prescribed word limit). A large feature value or ratio implies good use of vocabulary only in cases
187 where the essay is of a sufficient length this influencing the final grade in a positive manner.

188 **Semantic Similarity (two features)** We propose two features on semantic similarity and coherency.
189 Semantic similarity of the essay content with the topic and semantic similarity and coherency
190 between terms in the essay body. These two separate features determine to what extent the essay is
191 coherent as well as relevant to the given topic. The concept of semantic similarity is being used in
192 two features to judge both relevance of the essay to the topic and the coherence of the essay itself. It
193 is being calculated by using WordNet⁷ and NLTK library. The text is first tokenised into sentences
194 and for each pair of sentences, their semantic similarity is computed using a multi-step process.

195 Step 1: Term pairs are formed and represented as (i,j) such that i belongs to the first sentence and j
196 belongs to the second sentence. The root of both words (I and j) are compared. A semantic score is
197 assigned to the pair by using the WordNet and NLTK library term similarity function. This process
198 is repeated for all possible pairs for the two sentences.

199 Step 2: Out of all such scores computed in Step 1, the highest score is taken to be the semantic
200 similarity of the two sentences. We repeat the process (Step 2) for all pairs of sentences in the
201 document.

202 Step 3: The semantic similarity score of the entire piece of text (either paragraphs or the document
203 as a whole) is computed by taking the average of the semantic similarity scores assigned to each
204 pair of sentences.

205 Step 4: The average score obtained in the previous step is then multiplied by the log (to the base
206 2) of the number of sentences. This normalisation is done to ensure that essays with very few
207 sentences (and thus far away from the specified word count) do not receive high scores.

208 Semantic Similarity of the essay with the topic: this feature evaluates the relevance of the essay
209 to the given topic by computing the semantic similarity of each sentence from the topic and each
210 sentence from the essay. A high score implies that the essay is fairly relevant to the topic.

211 Semantic Similarity of the essay: this feature evaluated the coherence of the essay itself by
212 computing the semantic similarity of each sentence of the essay to every other sentence of the essay.
213 A high score implies that the essay is fairly coherent.

214 There is a wide range of supervised learning algorithms. Following are the three classifiers used in our
215 experiments:

216 **kNN** k-Nearest Neighbour has been widely used in text classification problems. It is a simple and efficient
217 approach. It is called as a lazy learner as it only stores all the training examples in the learning
218 phase. It does not build a statistical model in the training phase. It does the classification by finding
219 the k-closest training examples and doing a weighted or majority vote for predicting the target class
220 (Tan, 2006).

221 **Linear Regression** Linear regression based approaches can be used for text classification (Zhang and
222 Oles, 2001). Linear regression based classifier works by selecting a linear discriminant function
223 and then selecting a threshold value for classification (Zhang and Oles, 2001).

224 **SVM** Support Vector Machines are supervised learning models and have been used in several types of
225 text classification problems (Smola and Schölkopf, 2004). SVM classifier works by creating a
226 hyperplane separating the instances (represented as points in a space) of the target classes in an
227 n-dimensional feature space. SVM method is good for both linear and non-linear classification
228 problems (Smola and Schölkopf, 2004).

229 There is a wide range of feature selection and ranking techniques. We use the following two approaches
230 in our experiments.

⁷<https://wordnet.princeton.edu/>

| Essay Set | GSR | NTE | NSE | AWC | ASC |
|-----------|------|------|-----|--------|-------|
| Set-1 | 2-12 | 1783 | 589 | 365.89 | 22.78 |
| Set-7 | 0-30 | 1569 | 441 | 168.12 | 11.65 |
| Set-8 | 0-60 | 723 | 233 | 609.39 | 34.86 |

Table 1. Overview of Experimental Dataset. GSR: Grade Score Range, NTE: Number of Training Essays, NSE: Number of Test Essays, AWC: Average Word Count, ASC: Average Sentence Count

231 **RELIEF** RELIEF is a widely used feature selection algorithm and is based on taking into account
 232 the attribute inter-relationship by computing values such as correlation and covariance (Kira and
 233 Rendell, 1992)(Kononenko, 1994)(Robnik-Sikonja and Kononenko, 1997). It is based on the
 234 concept of attribute estimation in which a relevance grade is assigned to each of the features and
 235 selection is based on a threshold value (Kira and Rendell, 1992)(Kononenko, 1994)(Robnik-Sikonja
 236 and Kononenko, 1997)

237 **Correlation-based Feature Subset Selection (CFS)** This technique was proposed by Hall et al. (Hall,
 238 1998). CFS computes the importance of a subset of attributes by evaluating the individual predictive
 239 ability of each of the attributes along with the degree of redundancy between the attributes (Hall,
 240 1998).

241 There are 9 features or independent variables for our classification problem. The range and scale of all
 242 the independent variables are different and hence we apply techniques to standardize the range of our
 243 independent variables. Data normalization and scaling is an important data pre-processing step and is
 244 done before applying the classification algorithms (Graf et al., 2003). We rescale the range of 9 features
 245 to a scale in the range of 0 to 1.

246 2.2 Experimental Dataset

247 In this work, we used publically available Hewlett Foundation's Automated Student Assessment Prize
 248 (ASAP) dataset for experimental evaluation. Users can freely sign-up on Kaggle and download this
 249 dataset. This dataset has been extensively used in literature for evaluating automatic grading techniques
 250 (Dong and Zhang, 2016)(Cummins et al., 2016). ASAP dataset is divided into 8 sets, where each set has a
 251 different domain. This ensures variability of domain in dataset. Each set comprises labelled training and
 252 testing essay data. All essays have been hand graded by 2 to 3 instructors and based on the combined
 253 scores of instructors, a final grade has been assigned. We use a publicly available dataset to enable easier
 254 reproducibility and replicability of our results (Stodden, 2012)(Vitek and Kalibera, 2011). We believe
 255 that experiments on automated essay scoring should be done on a shared data so that the approaches can
 256 be compared and improved by other researchers than the inventors of a particular approach (Stodden,
 257 2012)(Vitek and Kalibera, 2011).

258 Each essay set has a different grade score range (Set 1: 2-12, Set 2: 1-6, Set 3: 0-3, Set 4: 0-4, Set
 259 5: 0-4, Set 6: 0-4, Set 7: 0-30, Set 8: 0-60). Out of 8 available essay sets, we used 3 essay sets (Set 1,
 260 Set 7 and Set 8). We selected the essay sets which have highest grade range for experimental evaluation.
 261 This allows a wide distribution of grade levels. Overall, we used a total of 4075 essays for training and
 262 1263 essays for testing. Table 1 presents an overview of the experimental dataset. Table 1 shows that
 263 the number of training essays is 1783 for Set 1. The number of training essays for Set 1 is the highest
 264 amongst the three sets. Table 1 displays the average word count and sentence count for the essays in the
 265 three sets. We observe that the average sentence count varies from 11 to 34 across the three sets in our
 266 experimental dataset. Table 1 shows that the number of test essays are sufficient to evaluate the accuracy
 267 of the proposed approach. We believe that our dataset is diverse (three different sets) and large (4075) to
 268 increase the generalizability of our results.

269 3 RESULTS

270 3.1 Feature Distribution

271 Table 2 shows the descriptive statistics presenting the summary of the 9 features in-terms of the central
 272 tendency, dispersion and spread for Set 1. Table 2 shows that the median value for the *Vocabulary* is
 273 0.23 and the Tense is 0.56. The median values shows in Table 2 is the measure of the centrality and can

| | Attribute | Min | Q1 | Median | Q3 | Max |
|---|---------------------------------|------|------|--------|------|------|
| 1 | Vocabulary | 0.01 | 0.18 | 0.23 | 0.29 | 0.61 |
| 2 | Word Count Limit Ratio | 0.00 | 0.15 | 0.28 | 0.43 | 0.98 |
| 3 | Semantic Similarity Topic Essay | 0.00 | 0.92 | 1.02 | 1.11 | 1.57 |
| 4 | Voice | 0.72 | 0.96 | 0.98 | 1.00 | 1.00 |
| 5 | Semantic Similarity Essay | 0.00 | 1.03 | 1.16 | 1.31 | 2.07 |
| 6 | Spell Errors | 0.00 | 0.02 | 0.03 | 0.04 | 0.53 |
| 7 | Tense | 0.35 | 0.50 | 0.56 | 0.62 | 1.00 |
| 8 | Grammatical Errors | 0.00 | 0.01 | 0.02 | 0.03 | 0.11 |
| 9 | Long Sentences | 0.00 | 0.33 | 0.46 | 0.60 | 1.00 |

Table 2. Descriptive Statistics for 9 Features for Set 1

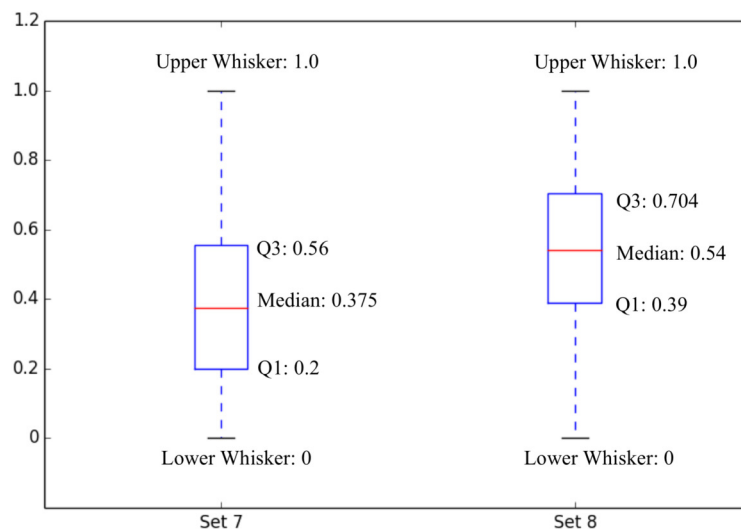


Figure 2. Boxplot for the Attribute Long Sentences for Set 7 and Set 8

274 provide insights on the skewness of the data. Table 2 displays the first and third quartile values ($Q1$ and
 275 $Q3$) which can be used to compute the interquartile range indicating the variability around the mean. We
 276 compute the descriptive statistics in Table 2 to observe data patterns and generate hypothesis. We show
 277 the descriptive statistics in Table 2 for only one Set (Set 1) as an illustration. We observe variability and
 278 spread in the feature values for the other Sets also. Table 2 shows that the $Q1$ value of Voice is 0.96 and
 279 the $Q1$ value of the Spell Errors is 0.02. We observe that the $Q3$ value of Semantic Similarity Topic Essay
 280 is 1.11. From the numerical summary we infer that the values for the 9 features are scattered and have a
 281 spread. The feature values are diverse and contains several values between the largest and the smallest.

282 Figure 2 and 3 shows the boxplots for displaying and comparing the distribution of two attributes
 283 across two datasets. Figure 2 shows a comparison of the attribute Long Sentences for Set 7 and Set 8.
 284 Figure 3 shows a comparison of the attribute Tense for Set 7 and Set 8. The boxplot in Figures 2 and 3
 285 presents the five number summary: minimum, first quartile, median, third quartile, and maximum. Figure
 286 2 reveals that the median value of Long Sentences for Set 8 is higher than the medial value for Set 7.
 287 Similarly the $Q1$ and $Q3$ values of Long Sentences for Set 8 is higher than the $Q1$ and $Q3$ values for Set
 288 7. The datasets in Figures 2 and 3 spans the same range since we normalized the values (between 0 and
 289 1). The boxplots in in Figures 2 and 3 in comparing the distributions and shows that there is a variation
 290 in the values of a feature across datasets and within a dataset. The boxplot in Figure 3 reveals a very
 291 less difference in the middle portion of the feature values across the two Sets. The Tense value of 0.518
 292 divides the dataset into two halves for Set 7 and the tense value of 0.459 divides the dataset into two

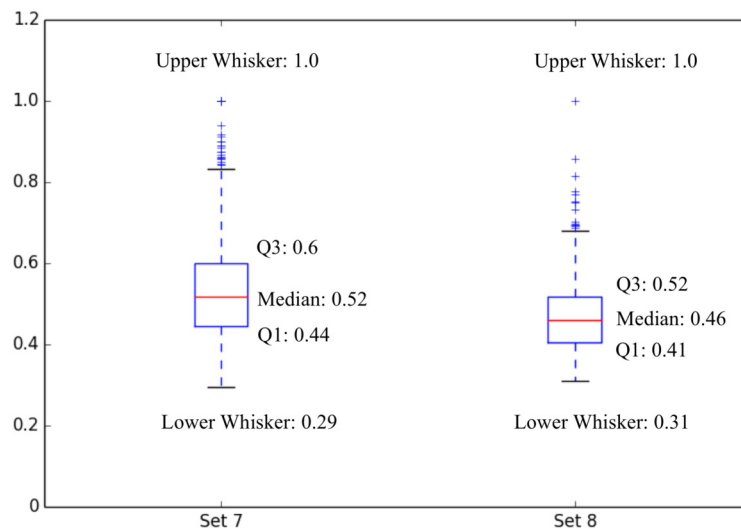


Figure 3. Boxplot for the Attribute Tense for Set 7 and Set 8

293 halves for Set 8. The interquartile range denotes the middle half of the dataset. The interquartile range
 294 and the data distribution of Tense feature shows a similar skewness pattern. We observe that both the
 295 boxplots shows a symmetric skewness pattern which is important to understand from the perspective of
 296 building predictive models.

297 3.2 Feature Selection

| Item | Quantity | Attribute |
|------|------------|---------------------------------|
| 1 | 0.0065584 | Vocabulary |
| 2 | 0.0047464 | Word Count Limit Ratio |
| 3 | 0.0026625 | Semantic Similarity Topic Essay |
| 4 | 0.002551 | Voice |
| 5 | 0.0007761 | Semantic Similarity Essay |
| 6 | 0.0007395 | Spell Errors |
| 7 | 0.0004207 | Tense |
| 8 | 0.0000431 | Grammatical Errors |
| 9 | -0.0018502 | Long Sentences |

Table 3. Ranking Results from Relief Feature Selection Algorithm

298 Feature selection is an important pre-processing step in the machine learning based classification
 299 data processing pipeline. We apply feature selection to identify features which are informative and
 300 remove redundant or irrelevant features. We use two different features selection techniques (1) RELIEF
 301 (2) Correlation-based Feature Subset Selection (CFS). Our objectives behind the application of feature
 302 selection technique is to also gain insight about the strength of relationship between the feature and the
 303 target class. We apply two different types of feature selection techniques: one of the techniques ranks the
 304 features (RELIEF) and the other technique does not rank but identifies a subset of most relevant features
 305 (CFS). We use RELIEF feature selection algorithm which can be applied to both binary and continuous
 306 data (Kira and Rendell, 1992)(Kononenko, 1994)(Robnik-Sikonja and Kononenko, 1997). RELIEF was
 307 proposed by Kira and Rendell et al. (Kira and Rendell, 1992) and then updates to the algorithm was made
 308 by Kononenko et al. (Kononenko, 1994). We use the updated version of the RELIEF feature selection
 309 algorithm implemented in Weka machine learning software. RELEIF based feature selection techniques
 310 are able to detect feature dependencies also. RELEIF algorithm evaluates the importance or worth of the

Confusion Matrix for Set 1 (kNN Classifier)

| | | Predicted Class | | | |
|--------------|---------|-----------------|---------|---------|---------|
| | | Class A | Class B | Class C | Class D |
| Actual Class | Class A | 75 | 66 | 0 | 0 |
| | Class B | 19 | 380 | 13 | 0 |
| | Class C | 0 | 8 | 26 | 0 |
| | Class D | 0 | 0 | 0 | 2 |

Confusion Matrix for Set 7 (SVM Classifier)

| | | Predicted Class | | | |
|--------------|---------|-----------------|---------|---------|---------|
| | | Class A | Class B | Class C | Class D |
| Actual Class | Class A | 10 | 2 | 0 | 0 |
| | Class B | 8 | 237 | 55 | 0 |
| | Class C | 0 | 27 | 100 | 0 |
| | Class D | 0 | 0 | 2 | 0 |

Confusion Matrix for Set 8 (kNN Classifier)

| | | Predicted Class | | | |
|--------------|---------|-----------------|---------|---------|---------|
| | | Class A | Class B | Class C | Class D |
| Actual Class | Class A | 1 | 1 | 0 | 0 |
| | Class B | 9 | 210 | 4 | 0 |
| | Class C | 0 | 2 | 6 | 0 |
| | Class D | 0 | 0 | 0 | 0 |

Table 4. Confusion or Error Matrix for the Best Performing Classifier on a Dataset

311 feature and assigns a weight to it. Table 3 shows the rank of the nine features selected from an initial
 312 list of 15 features and their corresponding weights assigned by the RELIEF algorithm. The weights are
 313 computed by a process of repeatedly sampling an instance in the dataset and analysing or computing the
 314 value of the given feature for the nearest neighbour of either the same or the differential class (Kira and
 315 Rendell, 1992)(Kononenko, 1994)(Robnik-Sikonja and Kononenko, 1997). Table 3 reveals that the top 5
 316 attributes are: Vocabulary, Word Count Limit Ratio, Semantic Similarity Topic Essay, Voice and Semantic
 317 Similarity Essay.

318 Correlation-based Feature Subset Selection (CFS) was proposed by Hall et al. (Hall, 1998). CFS
 319 computes the importance of a subset of attributes by evaluating the individual predictive ability of each
 320 of the attributes along with the degree of redundancy between the attributes (Hall, 1998). According
 321 to the CFS technique, subsets of features or attributes in the dataset that are highly correlated with the
 322 target class while having low inter-correlation or inter-association are preferred (Hall, 1998). The result
 323 of applying CFS was the subset containing four attributes: Long Sentences, Tense, Semantic Similarity
 324 Topic Essay and Vocabulary. In our case, ReliefF ranks Vocabulary and Word count limit ratio very high.
 325 These two attributes have a good correlation and hence only one of them (Vocabulary) appears in the
 326 subset that CFS output. CFS algorithm selects 4 attributes out of which both the algorithms agree on
 327 2 attributes i.e., Vocabulary and Semantic Similarity Topic Essay. This indicates that the two attributes
 328 are good predictors of the essay score. The subset produced by CFS contains Long Sentences as well as
 329 Tense which are ranked relatively low by RELIEF. This is due to the fact that CFS also checks for low
 330 intra-correlation but Relief ranks them individually.

331 3.3 Confusion or Error Matrix

332 Table 4 shows the confusion or error matrix displaying the performance of the best performing classifier
 333 on a particular dataset. We discretize the score into four categories: A, B, C and D. For example, in-case
 334 of Set 1 an 'A' grade represents a score of 10-12, 'B' grade represents a score of 7-9, 'C' grade represents
 335 a score of 4-6 and 'D' grade represents 2-3. The row represents the actual class and the column represents
 336 the predicted class. Table 4 reports the false positives, false negatives, true positives, and true negatives
 337 for every category. The confusion matrix is for the test data and shows that the kNN classifier on Set 1

| Set | Grade | CCI | INC | ACC | OSACC |
|-------|---------|-----|-----|--------|--------|
| Set 1 | Grade A | 75 | 66 | 53.19% | 82.00% |
| | Grade B | 380 | 32 | 92.23% | |
| | Grade C | 26 | 8 | 76.47% | |
| | Grade D | 2 | 0 | 100% | |
| Set 7 | Grade A | 10 | 2 | 83.33% | 78.68% |
| | Grade B | 237 | 63 | 79.00% | |
| | Grade C | 100 | 27 | 78.74% | |
| | Grade D | 0 | 2 | 0% | |
| Set 8 | Grade A | 1 | 1 | 50% | 93.13% |
| | Grade B | 210 | 13 | 94.17% | |
| | Grade C | 6 | 2 | 75.00% | |
| | Grade D | 0 | 0 | NA | |

Table 5. Accuracy Results for the Best Performing Classifier Across Grade Categories and Sets. CCI – Correctly Classified Instances, INC – Incorrectly Classified Instances, ACC – Accuracy, OSACC – Overall Set Accuracy. Results are for best performing classifier in each set. kNN for Set 1 and Set 8. SVM for Set 7.

| Essay Set | kNN | SVM | LR |
|-----------|--------|--------|--------|
| Set-1 | 82% | 79.62% | 80.30% |
| Set-7 | 73.69% | 78.68% | 77.32% |
| Set-8 | 93.13% | 90.98% | 91.41% |

Table 6. Overall Classification Accuracy for 3 Classifiers across 3 Dataset

338 correctly classified 380 instances of the test set actually belonging to the category ‘B’ and misclassified
 339 19 instances into ‘A’ and 13 instances into ‘C’. Table 4 provides a detailed analysis of the quality of the
 340 output of the classifier on the essay dataset. The mislabelled or misclassified instances are the off-diagonal
 341 elements. For example, for the SVM classifier for Set 7, the number 3, 8, 27 and 57 are off-diagonal
 342 elements which are misclassified by the SVM classifier. The diagonal elements represents the number
 343 of instances which are correctly classifiers. For example, for the SVM classifier for Set 7, 10, 100 and
 344 237 are correctly classified instances. A higher value of the diagonal elements and a lower value of the
 345 off-diagonal elements represents a good classifier. Table 4 reveals very encouraging results for the kNN
 346 classifier on Set 8. Table 4 reveals that the number of incorrect predictions for the kNN classifier on Set 8
 347 is very less. For example, in the case of category ‘B’, only 13 instances are misclassified whereas 210
 348 instances are correctly classified.

349 3.4 Performance Summary and Classifier Comparison

350 Table 5 shows the detailed performance results for the best performing classifier for the four classes and
 351 for the three Sets. Table 5 shows that the accuracy of the kNN classifier for Set 1 with respect to the
 352 class ‘B’ is 92.23%. The performance of the kNN classifier for Set 1 is low (53.19%) for class ‘A’ in
 353 comparison to the performance of the SVM classifier for for the same class. The performance of the
 354 SVM classifier for class ‘A’ is 83.33% for Set 7. The performance of the kNN classifier for class ‘B’ for
 355 Set 8 is 94.17%. Table 5 shows that the majority class is ‘B’ and class ‘D’ is a minority class. The best
 356 performing classifier for class ‘C’ is SVM with an accuracy of 78.74%. We observe an accuracy of above
 357 75% for the class ‘C’ by all the three best performing classifiers. It is not possible to provide much insight
 358 on the classification performance for the class ‘D’ as the number of test instances belonging to class ‘D’
 359 is very less.

360 Figure 4 displays a histogram to show a visual comparison of the overall accuracy of the three
 361 classifiers for the three dataset. The histogram in Figure 4 is derived from information in Table 6. Table
 362 6 and Figure 4 reveals that the overall accuracy for the classifiers kNN, SVM and LR for Set 1 is 82%,
 363 79.62% and 80.30% respectively. kNN is the best performing classifier for Set 1. However, the difference
 364 between the performance of the classifier in terms of the overall accuracy is less than 3%. The best

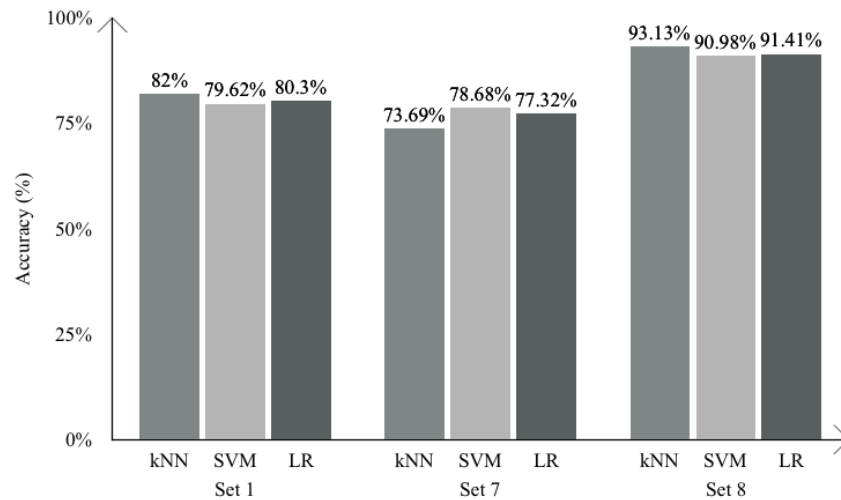


Figure 4. Histogram for Classifier Comparison

365 performing classifier for Set 7 is SVM with an accuracy of 78.68%. Table 6 and Figure 4 reveals that
 366 the overall accuracy for the classifiers kNN, SVM and LR for Set 8 is 93.13%, 90.98% and 91.41%
 367 respectively. kNN is the best performing classifier for Set 8. LR is the second best performing classifier
 368 for Set 8. We observe different accuracy for the three classifiers but the difference is not substantial and is
 369 within 5%. Based on the relative comparison of the three Sets, all classifiers exhibit high accuracy for Set
 370 8 and poor accuracy for Set 7. This result reveals that both the dataset and the classification algorithm
 371 influences the accuracy.

372 4 DISCUSSION

373 4.1 Interpretation of Findings and Recommendations

374 Our experimental results shows that it is possible to automatically estimate the writing quality and score
 375 of an essay written by school age students using natural language processing and machine learning
 376 techniques. The linguistic features as indicators or predictors depends on the essay rubric used by the
 377 human judge. For example, if grammar and mechanics (free from spelling, grammar and punctuation
 378 errors) is one of the criteria in the grading rubric then then using it as a feature in the machine learning
 379 framework will be useful. The score is a function of several features of varying relevance. Few features
 380 are more relevant and important than other features and it is interplay or combination of multiple feature
 381 values which determines the final score. We observed that both types of features are required: surface level
 382 features such as counting words and deep or more sophisticated features such as computing the coherence
 383 or writing style. Our insights reveal that it is important to perform feature scaling and normalization as the
 384 range and distribution of features vary. We observe that different classifiers result in difference accuracy.
 385 Hence more experiments (as future work) is needed to investigate the performance of more classifiers
 386 in addition to the three classifiers examined in our study in this paper. The overall accuracy also varies
 387 with the dataset. This shows that different features may be needed for different dataset as the grading
 388 rubric and level may have some variation across the dataset depending on the context such as the grade
 389 level. We observe some imbalance in the dataset with respect to the grade (A, B, C and D). There are very
 390 few essays with grade D and majority are in B and C. A and D grade is a minority class. In future data
 391 sampling techniques such as oversampling, under=sampling and SMOTE can be applied to counter the
 392 class imbalance problem to further enhance the performance of the essay grading the system. The class
 393 imbalance is natural as the grade often follows a normal distribution. Our results are encouraging and
 394 positive however more research is needed to investigate misclassified and incorrectly classified results.
 395 We believe that few misclassification can be corrected by making improvements to the system but few
 396 misclassifications are not due to the shortcoming of the automated essay grading system and rather due to
 397 subjectivity in evaluation and possible human errors.

398 4.2 Threats to Validity

399 There are several possible threats to validity in our experiments which we tried to minimize and mitigate
400 (internal and external validity threats) (Winter, 2000). We conduct experiments on multiple and diverse
401 dataset belonging to three different projects to investigate if our results are generalizable and hence
402 mitigate the threat to external validity. We downloaded a essay dataset from Kaggle repository which
403 is manually validated and of high quality. The dataset has been used in several experiments in the past
404 and our dataset selection is keeping mind that there are no annotation or measurement errors. However,
405 there is still a possibility of threats to internal validity in such empirical experiments. The impact on
406 the dependent variable (target clas) may not be completely attributed to the changes in the independent
407 variable (input features) because of overfitting of the predictive model. Another threat to validity is that
408 our 9 textual features may not be the only factor leading to writing skill or essay quality and there can be
409 other factors not included as part of our study presented in this paper.

410 5 CONCLUSIONS

411 We present machine learning and natural language processing based approach for automated essay grading.
412 We propose 9 surface level and deep linguistic features as predictors for the writing skill of the author
413 and quality of the essay in the context of Grade 7 to Grade 10. We conduct experiments on three sets
414 of publicly available and manually annotated dataset consists of more than 4000 essays across diverse
415 topics. We observe variability and spread in the feature values of the 9 attributes across 3 sets. We apply
416 two different types of feature ranking techniques. We conclude that features such as appropriate use of
417 vocabulary, word count with respect to the world limit, and relevance of the essay to the topic, coherency
418 in writing and correct usage of active and passive voice are good predictors of the essay score. We apply
419 there different classification algorithms to build predictive modes: k-nearest neighbour, support vector
420 machines and linear regression based classifier. Our analysis shows that the accuracy of the kNN classifier
421 for Set 1 with respect to the class 'B' is 92.23%. kNN is the best performing classifier for Set 1. The best
422 performing classifier for Set 7 is SVM with an accuracy of 78.68%. We observe different accuracy for the
423 three classifiers but the difference is not substantial and is within 5%. Our results on 4075 essays across
424 multiple topics and grade score range are encouraging with an accuracy of 73% to 93%.

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